Paper / Subject Code: 50602 / Applied Mathematics-III

Q. P. Code: 27250

(8)

S.E.(BIOTECHNOLOGY)(Sem III) (Choice Based) / 50602 - APPLIED MATHEMATICS- III)

Duration: 3 hrs Max. marks: 80

- 1. Question no.1 is compulsory
- 2. Answer **any three** from remaining.
- 3. Figures to the right indicate marks.
- 1.a. Find the Laplace transform of sint sin2t sin 3t (5)
- b. The proofs of a 500 page contain 500 misprints. Find the probability that (5) at least 4 misprints in a randomly chosen page.
- c. check whether this matrix is $A = \begin{bmatrix} 1 & -6 & -4 \\ 0 & 4 & 2 \\ 0 & -6 & -3 \end{bmatrix}$ is derogatory? (5)
- d. Find the analytic function whose imaginary part is $e^x \sin y$ (5)
- 2a. Show that $u = \left(r + \frac{a^2}{r}\right)\cos\theta$ is harmonic. Find $v(r, \theta)$ (6)
- b. Find $L\left(\sinh\left(\frac{\sqrt{3}}{2}t\right)\sin\left(\frac{t}{2}\right)\right)$ hence evaluate

$$\int_0^\infty e^{-t} \sinh\left(\frac{\sqrt{3}}{2}t\right) \sin\left(\frac{t}{2}\right) dt \tag{6}$$

c. Using Lagrangian multiplier , solve the N.L.P.P.

Optimize Z= $x_1^2 + x_2^2 + x_3^2$ subject to $x_1 + x_2 + 3x_3 = 2$,

$$5x_1 + 2x_2 + x_3 = 5, \quad x_1, x_2, x_3 \ge 0$$

- 3.a. Find the image of the region bounded by x = 0, x = 2, y = 0, y = 2 in the (6)
 - Z plane under the transformation w = (1+i)z
 - b. Show that $A = \begin{bmatrix} -9 & 4 & 4 \\ -8 & 3 & 4 \\ -16 & 8 & 7 \end{bmatrix}$ is diagonalisable .Find the diagonal

matrix and transforming matrix. (6)

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c. find the equations of lines of regression for the data given below.

X	5	6	7	8	9	10	110000
у	11	14	14	15	12		16

4.a. Solve N.L.P.P using Kuhn tucker conditions

(6)

(8)

Maximize Z= $2x_1^2 - 7x_2^2 + 12x_1x_2$ subject to $2x_1 + 5x_2 \le 98$, $x_1, x_2 \ge 0$

b. Using Convolution theorem find
$$L^{-1}\left[\frac{s^2}{(s^2+1)(s^2+4)}\right]$$
 (6)

c. Evaluate
$$\int_0^{\pi} \frac{d\theta}{3+2 \cos \theta}$$
 (8)

5.a Evaluate
$$\int_0^{1+i} z^2 dz$$
 along (i) the line $y = x$ (ii) the parabola $x = y^2$. (6)

Is the line integral independent of path? Explain.

b. Find the residues of
$$f(z) = \frac{\sin \pi z}{(z-2)(z-1)^2}$$
 at its poles (6)

c. Reduce the following quadratic form $q = X^T A X$ (8)

 $3x^2 + 5y^2 + 3z^2 - 2xy - 2yz + 2zx$ to canonical form by orthogonal transformation and hence find the rank, index and signature

6. a. Evaluate
$$\oint_C \frac{z+3}{2z^2+3z-2} dz$$
 where C is $|z-i|=2$ (6)

b.In 100 sets of 10 tosses of a coin in how many cases do you expect (6)

- (i) 7 head and 3 tails
- (ii) At least 7 heads

(8)

c.Find inverse laplace transform of by using partial fractions

$$\frac{s^2 + 16s - 24}{s^4 + 20s^2 - 64}$$
