## 1T01224 - S.E.(INFORMATION TECHNOLOGY) (Sem IV) (Choice Based)APPLIED MATHEMATICS - IV

(Hours: 3 hrs) [Total Marks: 80] **Note:** 1. Question no. 1 is compulsory. 2. Attempt any three questions out of remaining five questions. **Q.1.[a]** Given two lines of regression lines x + 2y - 5 = 0, 2x + 3y + 8 = 0. [5] Find (i)  $\bar{x}$ ,  $\bar{y}$  (ii) correlation coefficient r. **[b]** Show that  $97 \mid (2^{48} - 1)$ . [5] [c] The probability density function of a random variable x is zero except at [5]  $x = 0, 1, 2 \text{ and } p(0) = 3k^3, p(1) = 4k - 10k^2, p(2) = 5k - 1.$ Find (i) k (ii) p  $(0 \le x \le 2)$ . [d] Give an example of a graph which has [5] (i) Eulerian circuit but not a Hamiltonian circuit (ii) Hamiltonian circuit but not an Eulerian circuit Q.2.[a] Find gcd (2947, 3997) using Euclidean Algorithm. Also find x and y [6] such that  $2947x + 3997y = \gcd(2947, 3997)$ . [b] The four roots of unity 1, -1, i, -i forms a group under multiplication. [6] [c] Find whether the following graphs G = (V,E) and G' = (V',E') are [8] isomorphic? Justify. (1)  $V = \{a,b,c,d\}$ ,  $E = \{(a,b),(a,d), (b,d), (c,d),(c,b),(c,d)\}$ (2)  $V' = \{1,2,3,4\}$ ,  $E' = \{(1,2),(2,3),(3,1),(3,4),(4,1),(4,2)\}$ **Q.3.[a]** Show that  $(D_8, \leq)$  is a lattice. Draw its Hasse diagram. [6] [b] The local authorities in a certain city install 10,000 electric lamps in the [6] streets of the city. If these lamps have an average life of 1000 burning hours with a standard deviation of 200 hours, how many lamps might be expected to fail i) in the first 800 burning hours? ii) Between 800 and 1200 burning hours? [c] (i) Find inverse of  $2^{-1}$  (mod 31) using Fermat's theorem. [8] (ii) Find the Legendre's symbol of  $\left(\frac{19}{23}\right)$ . Q.4.[a] Calculate the coefficient of correlation between x and y from the [6] following data 11 12 | 9 | 8 | 10 y 14 8 6 9 11 12 3

[b] (i) Draw a connected graph for which every edge is a cut edge.

(ii) Show that any connected graph with 'n-1' edges is a tree.

**TURN OVER** 

[6]

2

[c]	<ul> <li>(i) Can it be concluded that the average lifespan of an Indian is more than 70 years if a random sample of l00 Indians has an average lifespan of 71.8 years with standard deviation of 8.9 years?</li> <li>(ii) Ten individuals are chosen at random from a population and their heights are found to be in inches 63, 63, 64, 65, 66,69, 69, 70, 70,71.</li> <li>Discuss the suggestion that the mean height of the universe is 65 inches.</li> </ul>	[8]
Q.5.[a]	Solve $x \equiv 5 \pmod{6}$ , $x \equiv 4 \pmod{11}$ , $x = 3 \pmod{17}$ .	[6]
[b]	Theory predicts that the proportion of beans in the four groups A, B, C, D should be 9:3:3:1. In an experiment among 1600 beans the numbers in the four groups were 882, 313, 287 and 118. Using Chi-Square verify does the experimental results support the theory?	[6]
[c]	Let G be a group of all permutations of degree 3 on 3 symbols 1, 2 & 3. Let $H = \{I, (1 \ 2)\}$ be a subgroup of G. find all the distinct left cosets of H in G and hence index of H.	[8]
Q.6.[a]	Show that $53^{103} + 103^{53}$ is divisible by 39.	[6]
[b]	Given $L = \{1, 2, 4, 5, 10, 20\}$ with divisibility relation. Verify that $(L, \leq)$ is a distributive but not complimented Lattice.	[6]
[c]	(i) Write the following permutation as the product of disjoint cycles $f = (1 \ 2) (1 \ 2 \ 3) (1 \ 2)$ .	[8]
	(ii) Express the expression $(x + y) (x + z) (x'y)'$ in the sum-of-product form.	