

- S.E.(ELECTRICAL)(Sem IV) (Choice Based) / 40604 - ELECTROMAGNETIC FIELD &amp; WAVE THEORY

Duration: 3Hrs

Marks: 80

**Note:** (1) Question No:1 is compulsory

(2) Attempt any three question from the remaining questions.

**Q1.** Solve any four from the remaining question. (20)

- State and explain Biot-Savart law.
- Explain current density and continuity equation.
- Convert P (10,  $\pi/6, \pi/3$ ) in cylindrical co-ordinates.
- Justify the statement "Divergence of a curl of a quantity is zero".
- Enlist five properties of electromagnetic wave.

**Q2.** (a) Evaluate both sides of divergence theorem for  $D = x^2\mathbf{a}_x + y^2\mathbf{a}_y + z^2\mathbf{a}_z$  over the cube  $0 < x, y, z < 1$ . (10)(b) Two uniform line charges of density 8.854nC/m are located in a plane  $z=0$  at  $y = \pm 6\text{m}$ . (10)

Find the E field at a point P (0, 0, 6).

**Q3.** (a) Derive Maxwell's equation in integral and point form for time varying field. (10)

(b) Derive the electric field intensity due to a infinite line charge. (10)

**Q4.** (a) Derive the Poisson's and Laplace equation. In Cartesian co-ordinates a potential is a function (10)of x only. At  $X = -20\text{cm}$ ,  $V = 25\text{V}$  and  $\mathbf{E} = -1.5 \times 10^3 \mathbf{a}_x \text{ V/m}$  throughout the region.Find V at  $X = 3 \text{ cm}$ .(b) A charge distribution in free space has  $\rho_v = 2r \text{ nC/m}^3$  in spherical co-ordinates, for  $0 < r < 10 \text{ m}$  (10)and zero otherwise. Determine  $\mathbf{E}$  at  $r = 2\text{m}$  and  $r = 12\text{m}$ .**Q5.** (a) Given that  $\mathbf{H} = \mathbf{H}_m e^{j(\omega t + \beta z)} \mathbf{a}_x$  (A/m) in free space, Find  $\mathbf{E}$ . (10)(b) A dielectric free space interface has the equation  $3X + 2Y + Z = 12\text{m}$ . The origin side of the interface has  $\epsilon_{r1} = 3$  and  $\mathbf{E}_1 = 2\mathbf{a}_x + 5\mathbf{a}_z$  (V/m). Find  $\mathbf{E}_2$  (10)**Q6.** (a) Transform given vector A in to cylindrical system  $\mathbf{A} = y\mathbf{a}_x + x\mathbf{a}_y + \frac{x^2}{\sqrt{x^2+y^2}} \mathbf{a}_z$ . (10)

(b) Starting from Maxwell equation obtain wave equation for the field E and H for free space. (10)

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