Paper / Subject Code: 29701 / Applied Mathematics - II.

1T01822 - F.E.(Sem II) (ALL BRANCHES)(Choice Based) / 29701 - Applied Mathematics - II

Time: 3 hours

Marks: 80

- N.B 1) Question **No. 1** is **Compulsory**.
 - 2) **Answer** any **three** questions from remaining questions.
 - 3) Figures to the right indicate full marks.
- Q.1 a) Evaluate $\int_0^\infty \frac{e^{-x^3}}{\sqrt{x}} dx$.
 - b) Find the length of the curve $x = \frac{y^3}{3} + \frac{1}{4y}$ from y = 1 to y = 2.
 - c) Solve $(D^2 + D)y = e^{4x}$.
 - d) Evaluate $\int_0^1 \int_{x^2}^x xy(x+y)dydx$.
 - e) Solve (4x + 3y 4)dx + (3x 7y 3)dy = 0.
 - f) Solve $\frac{dy}{dx} = 1 + xy$ with initial condition $x_0 = 0, y_0 = 0.2$ by Taylors series method. Find the approximate value of y for x=0.4 (step size 0.4).
- Q.2 a) Solve $\frac{d^2y}{dx^2} 16y = x^2e^{3x} + e^{2x} \cos 3x + 2^x$.
 - b) Show that $\int_0^{\pi} \frac{\log(1 + a\cos x)}{\cos x} dx = \pi \sin^{-1} a \ 0 \le a \le 1.$
 - Change the order of integration and evaluate $\int_0^2 \int_{2-\sqrt{4-y^2}}^{2+\sqrt{4-y^2}} dx dy$.
- Q.3 a) Evaluate $\iiint (x + y + z) dx dy dz$ over the tetrahedron bounded by 6 the planes x = 0, y = 0, z = 0 and x + y + z = 1.

b) Find the mass of the lamina bounded by the curves $y = x^2 - 3x$ and y = 2x if the density of the lamina at any point is given by $\frac{24}{25}xy$.

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- Solve $x^2 \frac{d^2y}{dx^2} + 3x \frac{dy}{dx} + 3y = \frac{logx \cdot cos(logx)}{x}$.
- Q.4 a) Find by double integration the area bounded by the parabola $y^2 = 4x$ and the line y = 2x 4.

b) Solve
$$\frac{dy}{dx} + x\sin 2y = x^3\cos^2 y$$
.

- Solve $\frac{dy}{dx} = x^3 + y$ with initial conditions y(0) = 2 at x=0.2 in steps of h=0.1 by Runge Kutta method of fourth order.
- Q.5 a) Evaluate $\int_0^1 x^5 \sin^{-1} x \, dx$ and find the value of $\beta\left(\frac{9}{2}, \frac{1}{2}\right)$.
 - b) In a circuit containing inductance L, resistance R, and voltage E, 6 the current i is given by $L\frac{di}{dt} + Ri = E$. Find the current i at time t if at t=0,i=0 and L,R, E are constants.
 - c) Evaluate $\int_0^6 \frac{dx}{1+3x}$ by using i) Trapezoidal ii) Simpsons (1/3)rd and iii) Simpsons (3/8)th rule.
- Q.6 a) Find the volume bounded by the paraboloid $x^2 + y^2 = az$ and the cylinder $x^2 + y^2 = a^2$.
 - b) Change to polar coordinates and evaluate $\int_0^1 \int_0^x (x+y) dy dx.$
 - c) Solve by method of variation of parameters $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = e^{e^x}.$

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