Paper / Subject Code: 29601 / Applied Mathematics - II.

1T01812 - F.E.(Sem II) (ALL BRANCHES)(REV.)(CBSGS) / 29601 - Applied Mathematics - II

Duration – 3 Hours

Total Marks: 80

- (1) N.B.:- Question no 1 is compulsory.
- (2) Attempt any THREE questions out of remaining FIVE questions.

1)a) Evaluate
$$\int_{0}^{\infty} \frac{dx}{(a^2 + x^2)^5}$$
 (4)

- b) Find the particular integral of $(D + 2)y = x^2$ (3)
- C) Solve $(\sin x \cos y + e^{2x})dx + (\cos x \sin y + \tan y)dy = 0$ (3)
 - Express the following integral in polar co-ordinates: (4)
- e) Prove that $E = 1 + \Delta$ (3)
- f) Evaluate $I = \int_{0}^{\pi/2} \int_{0}^{3(1-\cos t)} x^{2} \sin t \, dx \, dt$ (3)
- Solve $\frac{dy}{dx} xy = y^2 e^{-\left(\frac{x^2}{2}\right)} \log x.$ (6)
- b) Change the order of integration and evaluate $1 = \int_{0}^{1} \int_{1}^{\sqrt{2-y^2}} \frac{y \, dy \, dx}{\sqrt{\left(2-x^2\right)\left(1-x^2y^2\right)}}$ (6)
 - c) Evaluate $\int_{0}^{\pi} \frac{dx}{a+b\cos x}$ a > 0, |b| < a. Hence show that $\int_{0}^{\pi} \frac{dx}{(5+4\cos x)^2} = \frac{-4\pi}{27}$
- 3 a) Evaluate $I = \int_{0}^{\log 2} \int_{0}^{x} \int_{0}^{x+\log y} dx \, dy \, dz$ (6)
- b) Find the area between the circles $x^2 + y^2 4ax = 0$ and (6)

 $x^2 + y^2 - 2ax = 0$

Solve $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = \sin \log x$ (8)

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- 4 a) Find the total length of the curve $x = a e^{\theta} \sin \theta$, $y = a e^{\theta} \cos \theta$ from (6) $\theta = 0$ to $\theta = \frac{\pi}{2}$
 - b) Solve $(D^2 3D + 2)y = \frac{1}{e^{(e-x)}} + \cos\left(\frac{1}{e^x}\right)$ (6)
- Use Runge-Kutta method of fourth order, compute y(0.2) given $y' + y + xy^2 = 0$, y(0) = 1 by taking h = 0.1 correct to 4 decimal point.
- 5 a) State duplication formula and prove that $\sqrt{\frac{1}{4}} \sqrt{\frac{3}{4}} = \sqrt{2} \pi$ (6)
- b) Using Taylor's series method, obtain the solution of the differential equation y' = y xy, y(0) = 1 (6)
- Find the volume bounded by the paraboloid $z = 4 x^2 \frac{y^2}{2}$ and the plane z = 0.
- 6 a) A chain coiled up near the edge of a smooth table starts to fall over the edge. The velocity v when a length x has fallen is given by $x v \frac{dv}{dx} + v^2 = gx$. Show that $v = 8\sqrt{x/3}$
- b) Find the mass of a plate I the form of a cardioid $r = a(1 \cos \theta)$ if the density at any point of the plate varies as its distance from the pole.
- Evaluate $\int_{-3}^{3} x^4 dx$, using (i) Trapezoidal Rule (ii) Simpson's (1/3)rd rule. Compare it with exact solution.

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